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JEL : C49, C53

SARIMA:

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X ARIMA

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- 1- Bureau Census.
 - 2 - Ecclesiastical.
 - 3- Passover.
 - 4-Riazuddin, R. (January 2002);

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1 - Bell, W. R. and Hillmer, M. (1983).

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ARIMA

$$\Phi_P(B^s) \cdot \phi_p(B)(1-B)^d (1-B^s)^D x_t = \theta_q(B) \cdot \Theta_Q(B^s) \varepsilon_t \quad (1)$$

$\phi_p(B)$ $\theta_q(B)$ $\Phi_P(B^s)$ $\Theta_Q(B^s)$

P AR d, B p MA q D, AR Q MA

$$\begin{aligned} \phi_p(B) &= 1 - \phi_1 B - \phi_2 B^2 - \dots - \phi_p B^p \\ \Phi_P(B) &= 1 - \Phi_1 B^s - \Phi_2 B^{2s} - \dots - \Phi_P B^{Ps} \\ \theta_q(B) &= 1 - \theta_1 B - \theta_2 B^2 - \dots - \theta_q B^q \\ \Theta_Q(B^s) &= 1 - \Theta_1 B^s - \Theta_2 B^{2s} - \dots - \Theta_Q B^{Qs} \end{aligned}$$

به طور مثال الگوی $ARIMA(0,1,1) \times (0,1,1)_s$ به شکل رابطه زیر خواهد بود:

$$(1-B)(1-B^{12})x_t = (1-\theta B)(1-\Theta B^{12})\varepsilon_t$$

این الگو به کرات در پژوهش‌های مختلف در مدل‌های خطوط هوایی، تجارت و غیر بصورت یک فرایند سودمند بکار بسته شده است.

$\Theta_Q(B^s)$

, $\phi_p(B) = 0$ و $\Phi_p(B^s) = 0$ و $\theta_q(B) = 0$ و

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- 1 - Characteristic Equations.
 - 2 - Subjective.
 - 3 - Penalty Function Statistics.

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- 1 - Akaike Information Criterion.
 - 2 - Bayesian Information Criterion.
 - 3 - Final Prediction Error.
 - 4 - Hannan Quinn Criterion.
 - 5 - Fractional Indicator Variable.

ARIMA

$$\Phi_p(B^s) \phi_p(B)(1-B)^d (1-B^s)^D Z_t = \theta_q(B) \Theta_Q(B^s) a_t + \alpha_0 + \sum_{i=1}^n \beta_i D_{it} + \sum_j \gamma_j F_{ji} \quad ()$$

$$D_{it} = \begin{cases} 1 \\ 0 \end{cases}$$

$$F_{ji} = \frac{n_{ji}}{n_j} + \frac{n_{ji+1}}{n_j}$$

Z_t

$F_{ji} = 1$

$F_{ji} = 0$

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$$e^{i\alpha_j} \quad \alpha_j = \frac{2\pi j}{S} \quad j=1,2,\dots,S-1$$

$$-1; \pm i; -\frac{1}{2}(1 \pm \sqrt{3}i); \frac{1}{2}(1 \pm \sqrt{3}i); -\frac{1}{2}(\sqrt{3} \pm i); \frac{1}{2}(\sqrt{3} \pm i) \quad ()$$

$$\pm 5\pi/6 \quad \pm \pi/3 \quad \pm 2\pi/3 \quad \pm \pi/2, \pi \quad \pm \pi/6$$

B&M HEGY

$$\varphi(B) \quad () \quad S$$

$$\theta_1, \dots, \theta_s \quad \varphi(B) \quad :$$

$$\varphi(B) = \sum_{k=1}^S \lambda_k \Delta(B) / \delta_k(B) + \Delta(B) \varphi^{**}(B) \quad ()$$

$\varphi^{**}(B) \quad \lambda_k$

$$\Delta(B) = \prod_{k=1}^S \delta_k(B)$$

$$\varphi^*(B)$$

$$\theta_k$$

$$\varphi^*(B) y_{13t} = \sum_{k=1}^{12} \pi_k y_{n-t-1} + \varepsilon_t$$

$$\pi_k < 0$$

$$\pi_k = 0$$

$$\pi_k = 0$$

$$\pi_k = 0$$

$$\pi_k = 0$$

$$\pi_k = 0$$

$$\pi_{k-1} < 0$$

$$\pi_{k-1} = 0$$

$$\pi_{k-1} = \pi_k = 0$$

OLS

$\pi/2$

F

1 B&M(1993) PP.

2 -True Coefficient.

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Q (Statistic)

Q*

$$Q = n' \sum_{i=1}^k r_i^2(\hat{a}_i) \quad ()$$

$$Q^* = n' (n' + 2) \sum_{i=1}^k (n' + 1)^{-1} r_i^2(\hat{a}_i) \quad ()$$

S n n' = n - (d + s.D)

D d ()

i r_i^2 x_i^*

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n' = n , D = d = 0

Q*

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- 1 - Adequacy.
 - 2 - Box and Pierce.
 - 3 - Loung- Box.

$$r_i^2(\hat{a}_t)$$

Q^*
 Q^*

$$\hat{\varepsilon}_t$$

$$[\chi_{0.05}^2 (k - n_p)]$$

Q^*

x_t

SARIMA

SARIMA

AIC

ARMA

$$\{z_t\}_{1-d-D}^T$$

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ARIMA(p, d, q)(P, D, Q)_s

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- 1- Mills, T.C. (1999); Cambridge University Press.
 - 2 - Bower man B. and Richard T. O'Connell, (1987), "Time Series Forecasting".
 - 3 - Seasonal ARIMA.

: T

$$e_{T+h} = x_{T+h} - f_{T+h} = \varepsilon_{T+h} + \psi_1 \varepsilon_{T+h-1} + \dots + \psi_{h-1} \varepsilon_{T+1}$$

h $\psi_1, \dots, \psi_{h-1}$

. $\psi_p(B) = \alpha^{-1}(B) \theta(B) \Theta(B)$

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$$V(e_{T+h}) = \sigma^2 (1 + \psi_1^2 + \dots + \psi_{h-1}^2)$$

h h V(e_{T+h})

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/ (P)

$$d = D = 0$$

$$SARIMA(p, 0, q)(P, 0, Q)_{12}$$

t

		π	π	π	π	π	π	π	π	π	π	π	π					Q(36)	P-Value
	145.0302	-0.7453	-0.228	-0.792	-0.525	-0.389	-0.608	-3.062	-0.334	-3.886	-0.115	0.138	1.33					32.32	0.501
t	2.929716	-5.8237	-2.973	-7.018	-7.438	-6.278	-3.752	-5.906	-5.998	-5.808	-1.079	4.307	5.68	*	*	*	*		
	0.029282	-0.9218	-0.23	-0.839	-0.681	-0.685	-0.773	-3.718	-0.45	-4.814	-0.204	0.191	1.66					27.189	0.508
t	2.03412	-6.0134	-2.401	-6.314	-7.883	-8.034	-3.889	-5.997	-6.818	-6.005	-1.589	5.539	5.92	*	*	*	*		
	0.776757	-0.5975	-0.087	-0.609	-0.394	-0.316	-0.497	-2.463	-0.368	-2.996	0.008	0.036	0.93					37.649	0.306
t	2.003526	-5.6824	-1.664	-6.324	-6.961	-6.247	-3.855	-5.745	-7.182	-5.385	0.094	0.621	4.73	*	*	*	*		

تعداد وقفه ها در محاسبه Q برابر با ۳۶ است

SARIMA : ()

p-value			p-value			p-value		متغير
0.00	5.51	C	0.00	8.23	C	0.00	-2660.38	C
0.00	-0.08	D_FAR	0.10	0.01	RAMEZAN	0.00	-287.56	D_ORD
0.00	-0.13	D_ORD	0.00	0.01	@TREND^1.	0.00	-253.92	D_KHO
0.00	-0.09	D_KHO	0.00	0.06	D_FAR	0.00	421.45	D_MOR
0.03	-0.05	D_MOR	0.00	0.03	D_ORD	0.00	390.41	D_SHA
0.00	-0.15	D_TIR	0.00	0.02	D_BAH	0.00	-319.35	D_DEY
0.05	0.05	D_ABA	0.00	0.04	D_ESF	0.00	-299.19	D_BAH
0.02	0.06	D_AZA	0.00	-0.01	D_TIR	0.00	338.04	RAMEZAN
0.00	0.09	D_DEY	0.00	0.96	AR(1)	0.00	98.88	@TREND
0.00	0.08	D_BAH	0.00	-0.11	AR(13)	0.00	2263.03	DUM1_CHIKEN
0.01	0.06	D_MEH	0.00	0.78	SAR(12)	0.00	1431.33	DUM2_CHIKEN
0.00	0.18	@TREND^58	0.00	0.46	MA(1)	0.00	2287.17	DUM3_CHIKEN
0.00	0.09	ZIHAJEH	0.00	-0.90	SMA(12)	0.00	-964.35	DUM4_CHIKEN
0.00	0.75	AR(1)				0.00	1016.82	DUM5_CHIKEN
0.00	0.21	MA(1)				0.02	567.01	DUM7_CHIKEN
0.00	0.18	MA(27)				0.00	1545.21	DUM8_CHIKEN
0.01	-0.17	MA(29)				0.00	0.56	AR(1)
0.00	-0.29	MA(22)				0.01	-0.29	AR(26)
0.00	0.24	MA(6)				0.01	0.30	AR(27)
0.00	-0.20	MA(25)				0.05	-0.15	AR(20)
						0.00	0.47	SAR(12)
						0.00	-0.29	MA(15)
						0.07	-0.18	MA(3)

SARIMA

						0.04	-0.22	MA(8)
						0.00	-0.31	MA(18)
						0.00	0.30	MA(34)
						0.00	-0.88	SMA(12)
F-statistic		1571.37	F-statistic		37092.92	F-statistic		699.02
Prob(F-statistic)		0.00	Prob(F-statistic)		0.00	Prob(F-statistic)		0.00
Akaike info criterion		-2.35	Akaike info criterion		-5.53	Akaike info criterion		14.88
Schwarz criterion		-1.99	Schwarz criterion		-5.28	Schwarz criterion		15.44
R-squared		0.99	R-squared		1.00	R-squared		0.99
Adjusted R-squared		0.99	Adjusted R-squared		1.00	Adjusted R-squared		0.99
Q(36)		22.98	Q(36)		26.97	Q(36)		27.20
p_value		0.78	p_value		0.67	p_value		0.35

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AIC = /

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Q*() = /

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(0.37)

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*Q

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AIC

(0.48)

P=Q=0

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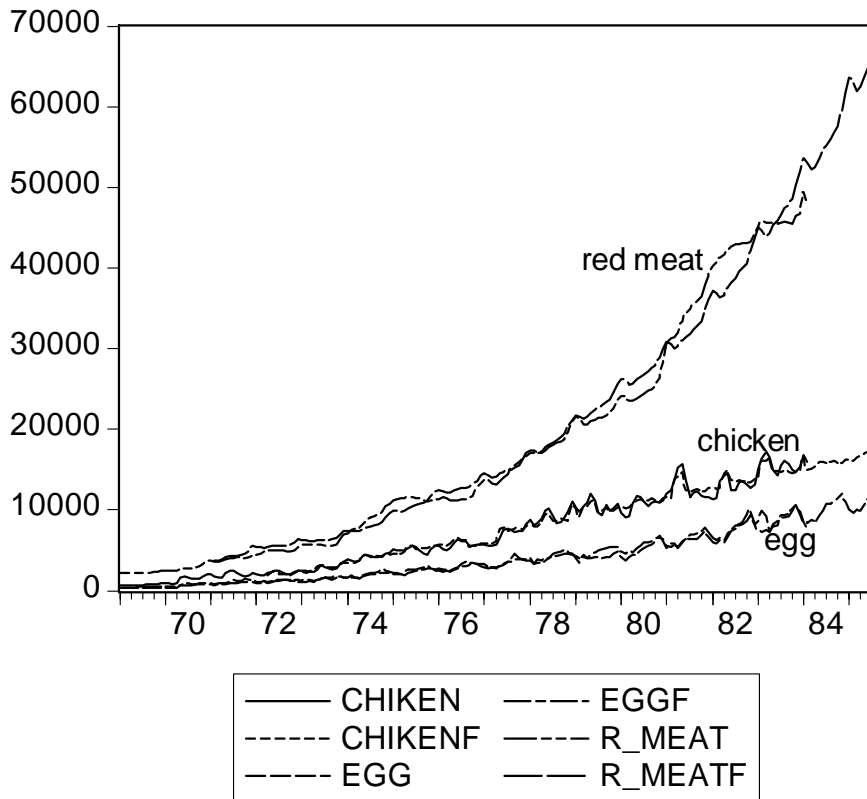
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گوشت مرغ			گوشت قرمز			تخم مرغ			
کران بالا	کران پایین	پیش‌بینی نقطه‌ای	کران بالا	کران پایین	پیش‌بینی نقطه‌ای	کران بالا	کران پایین	پیش‌بینی نقطه‌ای	زمان
16385.72	14652.82	15519.27	48098.25	45266.87	46682.56	9448.99	6996.03	8222.513	1384M03
16581.49	14587.86	15584.68	49531.63	44667.55	47099.59	9654.84	6364.46	8009.652	1384M04
16514.75	14391.65	15453.2	51432.83	45129.73	48281.28	11553.3	7221.65	9387.49	1384M05
16983.86	14956.92	15970.39	52837.76	45403.71	49120.74	12238.3	7435.44	9836.892	1384M06
16613.32	14638.75	15626.04	54296.47	45871.08	50083.78	12674	7573.42	10123.69	1384M07
17589.32	15517.76	16553.54	56024.97	46652.3	51338.64	13038.7	7723.44	10381.05	1384M08
17195.02	15174.8	16184.91	57570.8	47336.37	52453.58	13326.6	7744.8	10535.69	1384M09
16477.66	14517.7	15497.68	59122.31	48076.92	53599.62	13906.2	7997.29	10951.72	1384M10
16490.76	14557.9	15524.33	62337.79	50196.68	56267.24	14411.5	8225.95	11318.73	1384M11
17285.53	15375.32	16330.42	65713.09	52423.61	59068.35	13133.3	7471.27	10302.26	1384M12
16996.75	15012.54	16004.64	68780.86	54437.37	61609.12	11131.6	6217.54	8674.574	1385M01
16871.88	14888.8	15880.34	68569.43	53879.7	61224.56	12056.3	6772.14	9414.23	1385M02
16727.21	14545.16	15636.19	68403.2	53408.9	60906.05	13776.5	7745.35	10760.93	1385M03
17359.12	15149.01	16254.06	70039.55	54485.16	62262.36	12471.6	7013	9742.29	1385M04
17737.94	15547.49	16642.71	72677.66	56410.55	64544.11	14749.3	8317.41	11533.34	1385M05
18416.37	16263.13	17339.75	74621.81	57836.01	66228.91	15459.9	8734.07	12096.99	1385M06
18013.38	15894.96	16954.17	76574.65	59287.68	67931.17	15563.7	8786.64	12175.17	1385M07



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Census.

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